

FREE-STANDING MATHEMATICS QUALIFICATION ADVANCED LEVEL

Additional Mathematics

6993

Candidates answer on the Answer Booklet

OCR Supplied Materials:

- 16 page Answer Booklet
- Graph paper

Other Materials Required:

None

Tuesday 15 June 2010 Morning

Duration: 2 hours



INSTRUCTIONS TO CANDIDATES

- Write your name clearly in capital letters, your Centre Number and Candidate Number in the spaces provided on the Answer Booklet.
- Use black ink. Pencil may be used for graphs and diagrams only.
- Read each question carefully and make sure that you know what you have to do before starting your answer.
- Answer all the questions.
- You are permitted to use a scientific or graphical calculator in this paper.
- You are not allowed a formulae booklet in this paper.
- Final answers should be given correct to three significant figures where appropriate.

INFORMATION FOR CANDIDATES

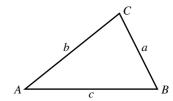
- The number of marks is given in brackets [] at the end of each question or part question.
- You are advised that an answer may receive no marks unless you show sufficient detail of the working to
 indicate that a correct method is being used.
- The total number of marks for this paper is 100.
- This document consists of 8 pages. Any blank pages are indicated.

Formulae Sheet: 6993 Additional Mathematics

In any triangle ABC

Cosine rule
$$a^2 =$$

Cosine rule
$$a^2 = b^2 + c^2 - 2bc \cos A$$



Binomial expansion

When n is a positive integer

$$(a+b)^n = a^n + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^2 + \dots + \binom{n}{r}a^{n-r}b^r + \dots + b^n$$

$$\binom{n}{r} = {^nC_r} = \frac{n!}{r!(n-r)!}$$

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Section A

1	Solve the inequality $3 - x < 4(x - 1)$.	[3]
2	Expand $(1-x)^{12}$ in ascending powers of x up to the term in x^3 , and simplify your answer.	[3]
3	The function $f(x)$ is defined by $f(x) = x^3 - 5x^2 + 2x + 8$.	
	(i) Find the remainder when $f(x)$ is divided by $(x + 1)$.	[2]
	(ii) Solve the equation $f(x) = 0$.	[3]
4	In a game 4 fair dice are thrown.	
	Calculate the probability that	
	(i) no six is thrown,	[2]
	(ii) at least 2 sixes are thrown.	[4]
5	The curve $y = x^3 - 3x^2 - 9x + 7$ has two turning points, one of which is where $x = 3$.	
	(i) Find the coordinates of the other turning point and determine whether it is a maximum minimum point.	or [5]
	(ii) Sketch the curve.	[1]
6	An aeroplane touches down at a point A on a runway, travelling at $90 \mathrm{ms^{-1}}$. It then deceler uniformly until it reaches a speed of $6 \mathrm{ms^{-1}}$ at a point B on the runway, $2016 \mathrm{m}$ from A.	ates

- - (i) Find the deceleration. [3]
 - (ii) Find the time taken to travel from A to B. [2]

7 It is required to solve the equation $\sin \theta \cos \theta = \frac{1}{4}$.

(i) Show that
$$\frac{\sin \theta}{\cos \theta} + \frac{\cos \theta}{\sin \theta} = \frac{1}{\sin \theta \cos \theta}$$
. [1]

- (ii) Hence show that the equation $\sin \theta \cos \theta = \frac{1}{4}$ is equivalent to $\tan \theta + \frac{1}{\tan \theta} = 4$. [2]
- (iii) By expressing this equation as a quadratic equation in t, where $t = \tan \theta$, find the two values of θ , in the range $0^{\circ} \le \theta \le 180^{\circ}$, that satisfy the equation. [4]
- A train moves between two stations, taking 5 minutes for the journey. The velocity of the train may be modelled by the equation $v = 60(t^4 10t^3 + 25t^2)$ where v is measured in metres per minute and t is measured in minutes.

Calculate the distance between the two stations. [5]

- **9** The diameter of a circle is PQ, where P and Q are the points (1, 3) and (15, 1) respectively.
 - (i) Find the centre of the circle. [2]
 - (ii) Show that the radius of the circle is $5\sqrt{2}$. [2]
 - (iii) Hence find the equation of the circle in the form $x^2 + y^2 + ax + by + c = 0$. [2]

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10 John and Paul are carrying out an experiment.

The table shows their results for x and y.

х	0	2	3	4
У	4	0	0.25	0

Paul proposes that the relationship should be modelled by y = k(x-2)(x-4). This is shown in Fig. 10.

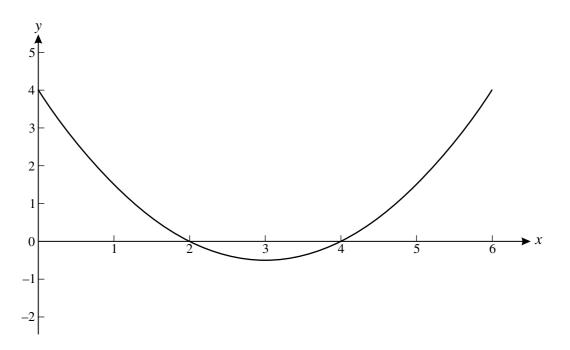


Fig. 10

- (i) Find the value of k for which the points (0, 4), (2, 0) and (4, 0) satisfy this equation. [2] John proposes a different model, using $y = c(x-2)^2(x-4)$.
- (ii) Find the value of c for which the points (0, 4), (2, 0) and (4, 0) satisfy this equation. [2]
- (iii) Which is the better model for John and Paul's results? Give a reason for your answer. [2]

Section B

Michael is at a point A and the base of a church tower is at a point F, as shown in Fig. 11. He measures the bearing of the tower to be 060°.

Michael walks 100 metres due North to the point B from where he measures the bearing of F to be 110° .

The triangle ABF is in the horizontal plane.

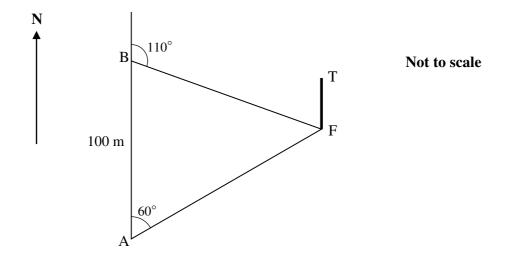


Fig. 11

(i) Show that AF = 122.7 m, correct to 4 significant figures, and find BF. [5]

Michael finds that the angle of elevation of the top of the tower, T, from A is 10°.

(ii) Find the height of the tower. [2]

C is the point on AB that is nearest to F.

(iii) Find CF and the angle of elevation from C to the top of the tower, correct to 1 decimal place.

[5]

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12 Fig. 12 shows the shape AOB that is to be made from card.

B is the point (5, 0) and OB is part of the curve with equation $y = 0.3x^2 - 1.5x$.

The line AB is the normal to the curve at B.

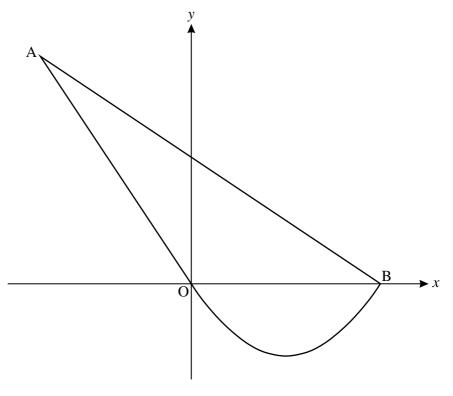


Fig. 12

(i) Find the equation of the line AB. [4]

The equation of the line AO is 2y + 3x = 0.

(ii) Find the coordinates of the point A. [3]

(iii) Find the area of the shape AOB. [5]

[Questions 13 and 14 are printed overleaf.]

13 Ali and Beth make components in a factory. Ali works faster than Beth and makes 3 more components per hour. As a result he takes 2 hours less time than Beth to make 72 components.

Let *t* hours be the time that Ali takes to make 72 components.

(i) Write expressions for the numbers of components made per hour by Ali and by Beth. [3]

[5]

- (ii) Hence derive the equation 3t(t+2) = 144.
- (iii) Solve this equation to find the times that Ali and Beth take to make 72 components. [4]
- 14 A firm has to transport 1500 packages to a site. It has a number of large vans which will transport 200 packages each and a number of small vans which will transport 100 packages each.

Let *x* be the number of large vans and let *y* be the number of small vans used.

(i) Write down an inequality based on the number of packages transported. [2]

The firm needs to use at least as many small vans as large vans.

- (ii) Write a second inequality. [1]
- (iii) Plot these two inequalities on a graph, using 1 cm to represent one van on each axis. Indicate the region for which these inequalities hold. Shade the area that is **not** required. [3]

A large van costs £80 to complete the trip and a small van costs £60 to complete the trip.

- (iv) Write down the objective function and hence find from your graph the number of each type of van that will minimise the cost, and work out that cost. [4]
- (v) What choice of vans should be made to minimise the cost if the restriction about the large and small vans is removed? Work out the cost in this case. [2]



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